

# State-Separating Proofs

## A Reduction Methodology for Real-World Protocols

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I sometimes suffer.

And the goal of this paper is to  
ease my suffering.

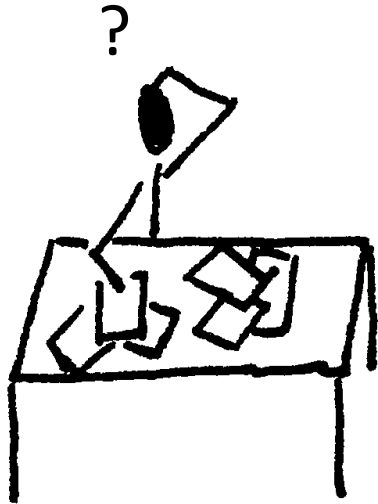
Key exchange researchers  
sometimes suffer.

And the goal of this paper is to  
ease our suffering.

Once upon a time...

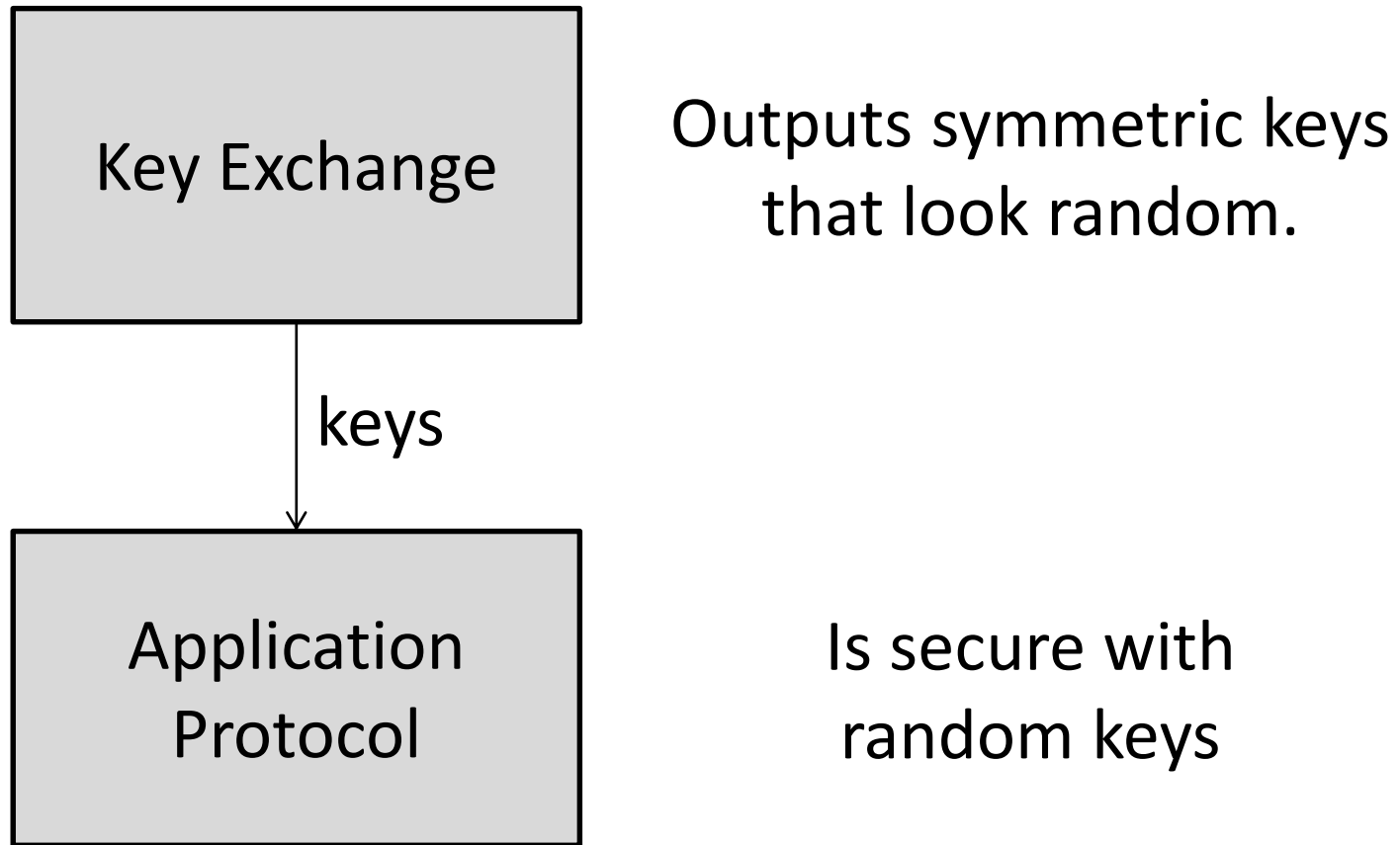
...I was a PhD student and I worked on key exchange.

At night, when I wrote proofs, I suffered.



- a) tons of work
- b) many *seemingly* simple steps
- c) not human-verifiable.

...one of the worst proofs was to prove that Bellare-Rogaway secure key exchange protocols are composable.





What I was really concerned about: The theorem seems so simple, why is the proof so hard?

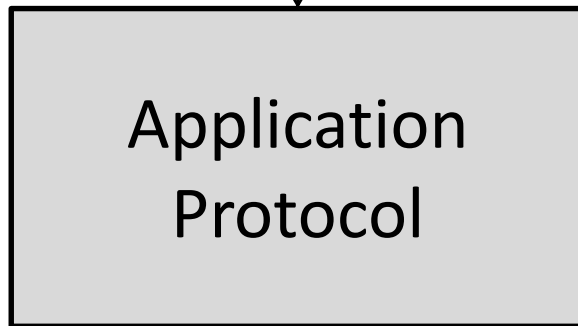
Tried in

CCS 2011 paper, my thesis, Stephen Williams's thesis...



Outputs symmetric keys  
that look random.

keys



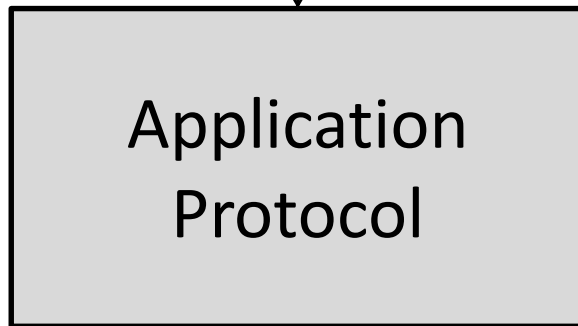
Is secure with  
random keys

# What is the difficulty?



Outputs symmetric keys  
that look random.

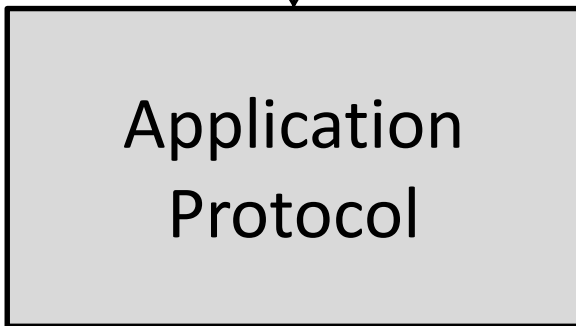
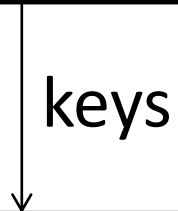
keys



Is secure with  
random keys



Outputs symmetric keys  
that look random.



Is secure with  
random keys

State is passed from one game to another, *defining* the composition is already annoying.

Key Exchange

Outputs symmetric keys that look random.

keys

Application Protocol

Is secure with random keys

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Key Exchange

keys

Application Protocol

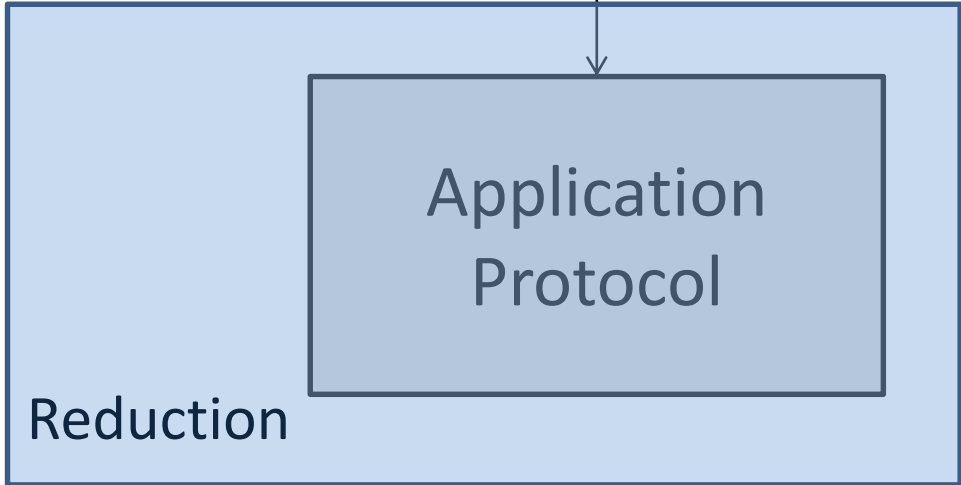
Outputs symmetric keys that look random.

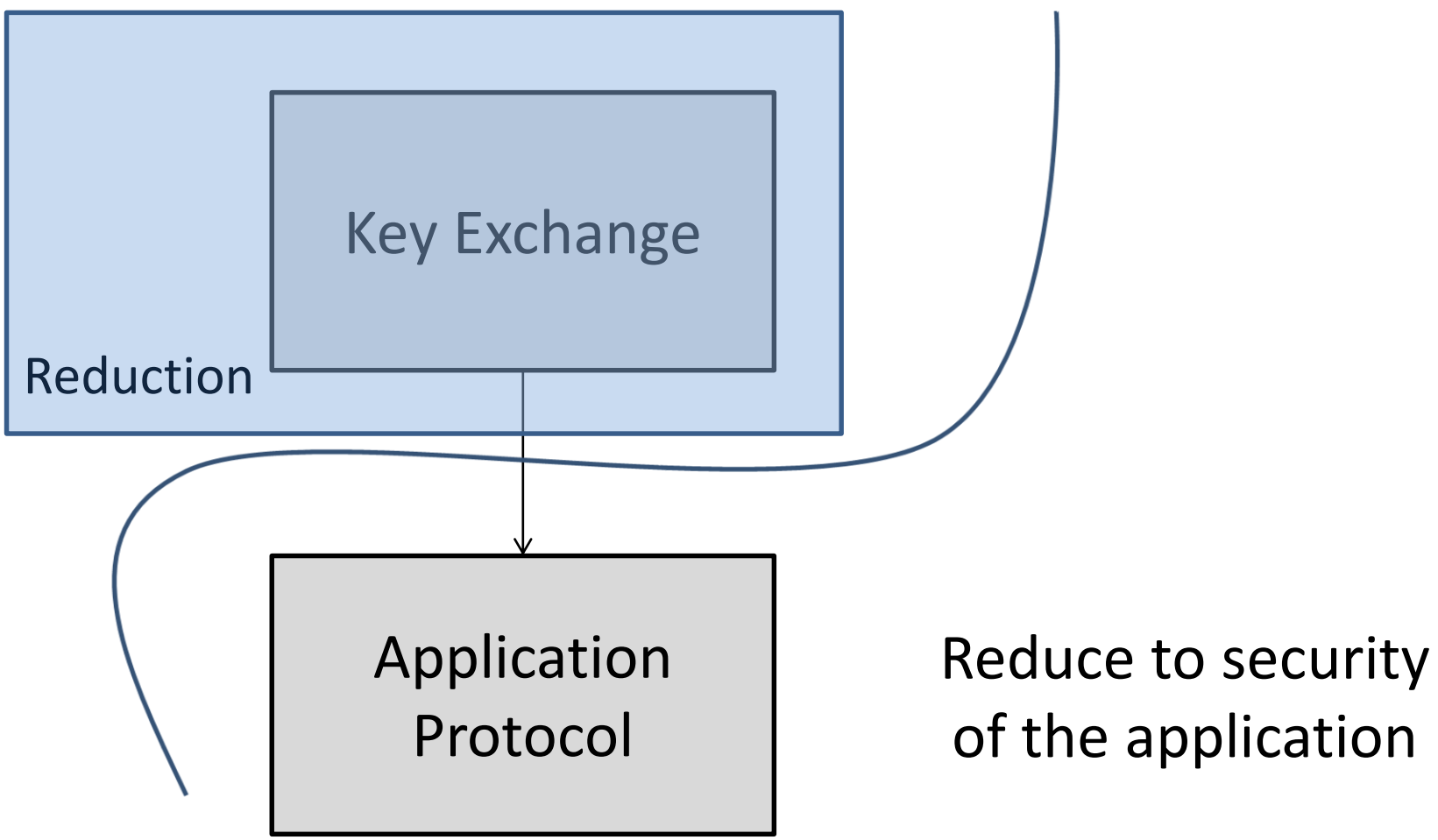
Multi-session & multi-instance

Is secure with random keys



Replace real keys  
with random keys







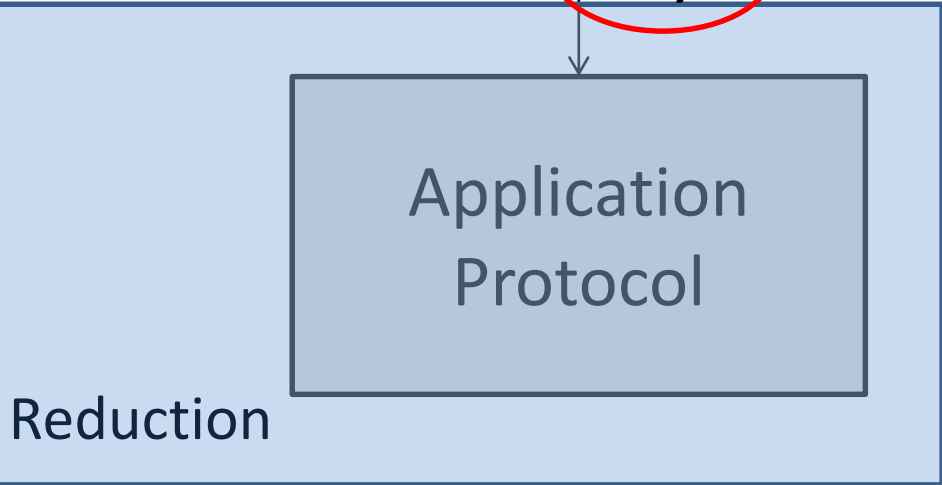
Replace real keys  
with random keys

keys

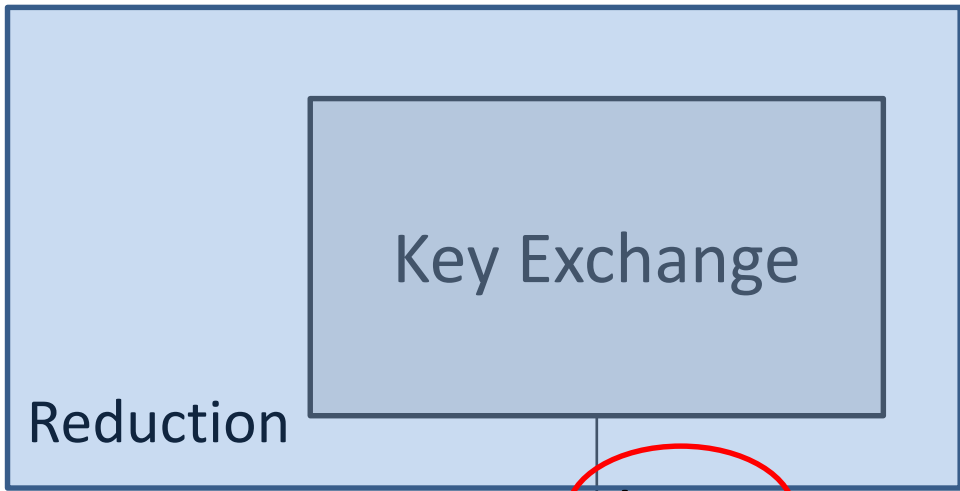
The word "keys" is written in black text and is circled in red.

Administrate lists in the  
reduction, pass on keys to  
the right sessions etc..

A red-bordered box containing red text.



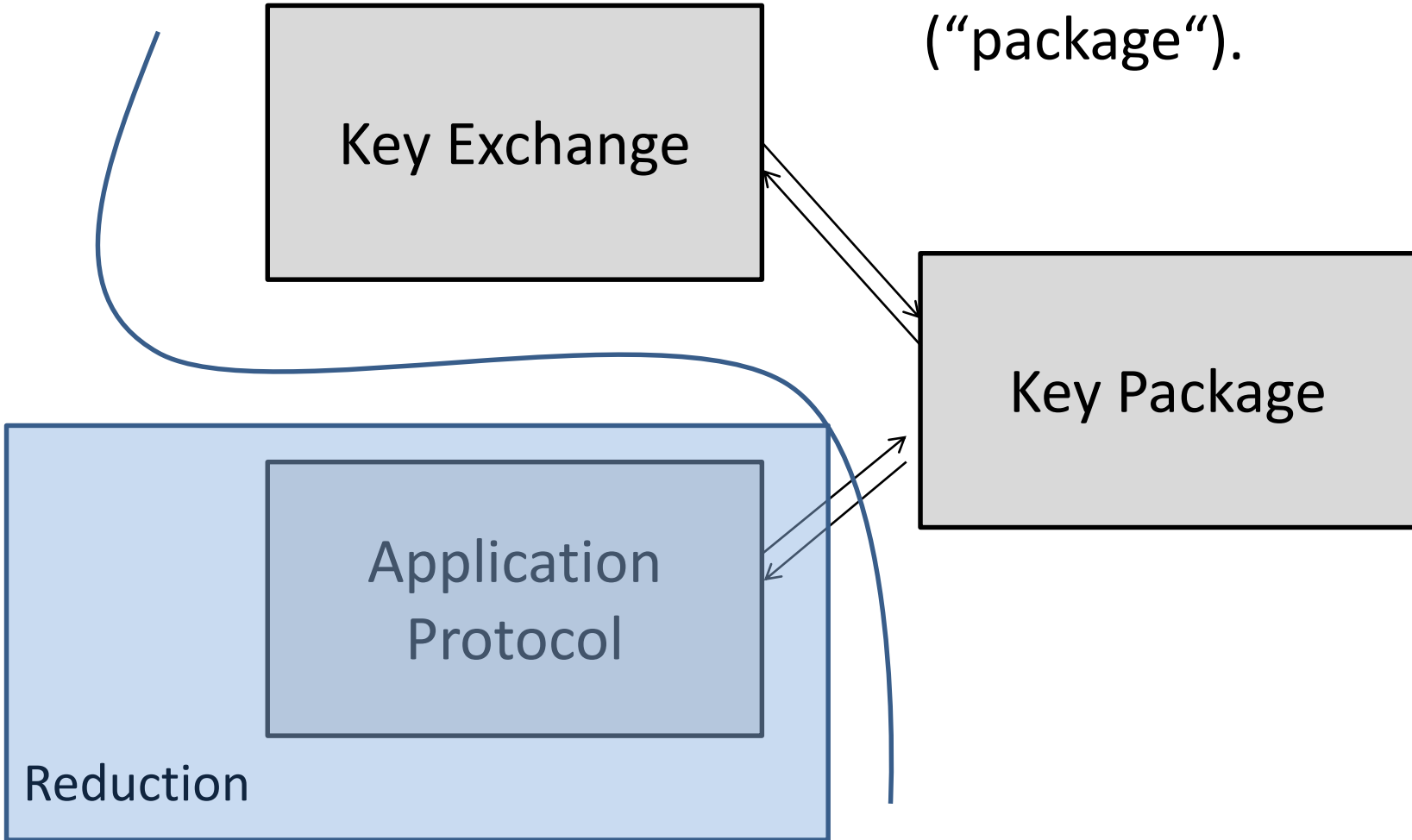




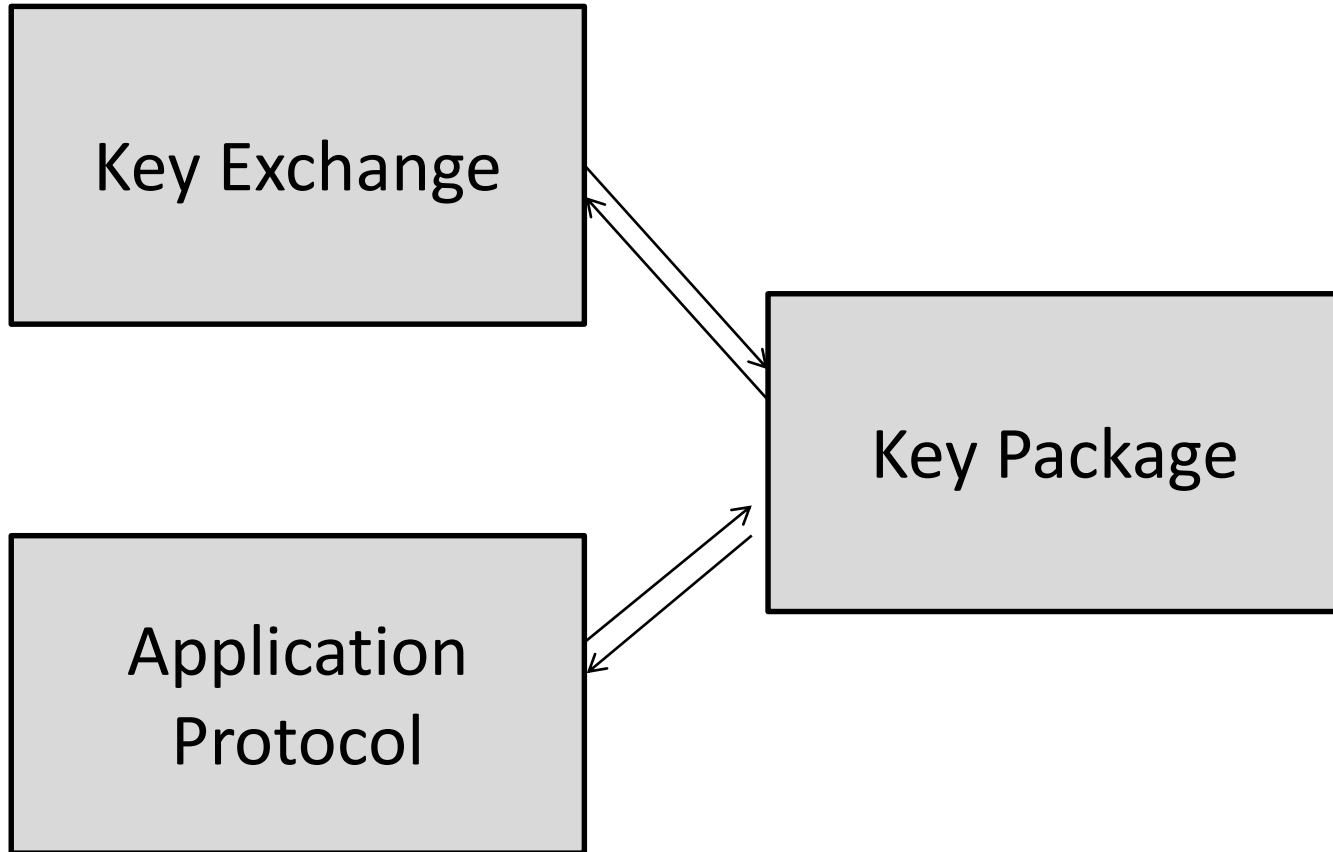
Administrate lists in the reduction, pass on keys to the right sessions etc..

Reduce to security of the application

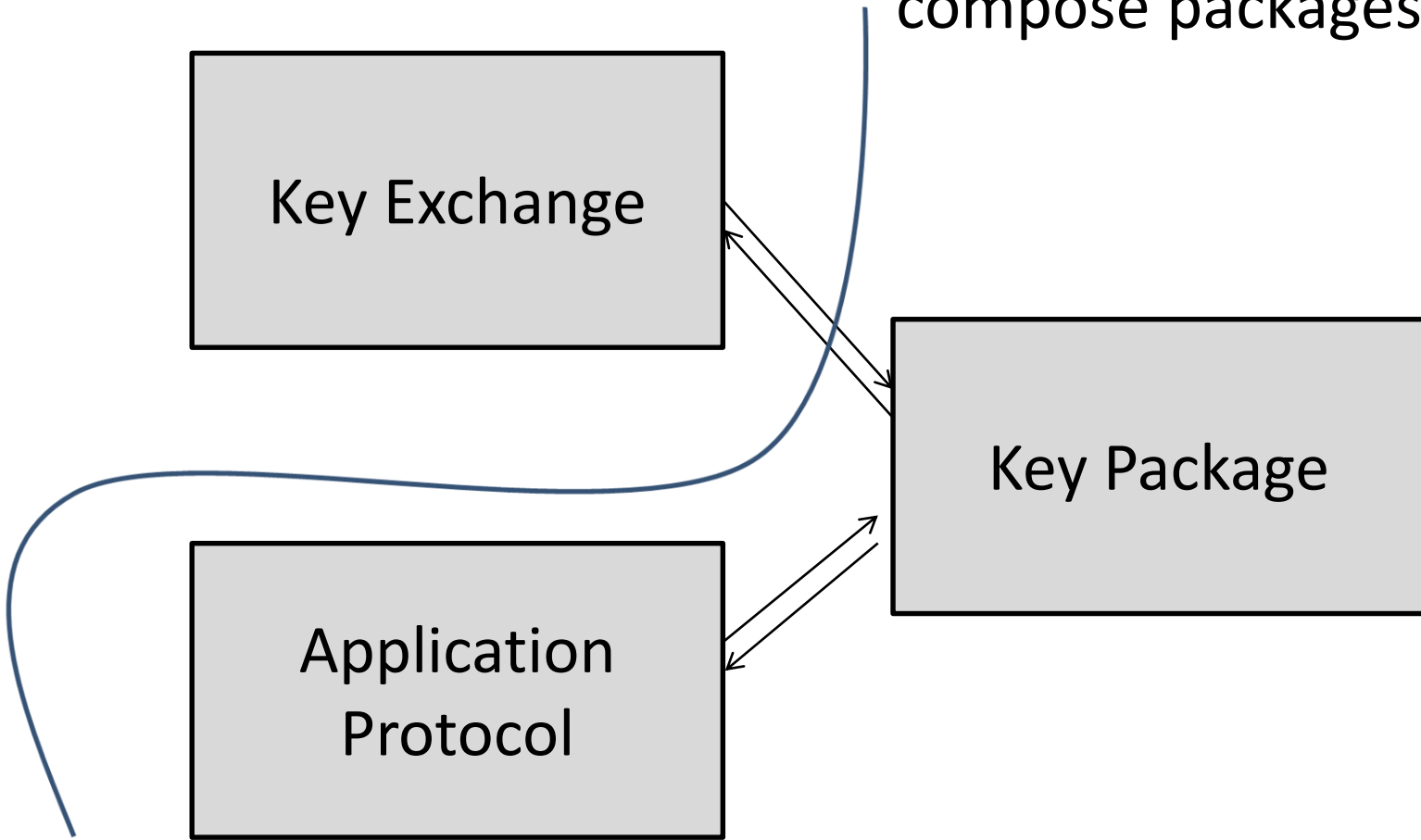
Idea 1: Move shared state to an external algorithm (“package”).



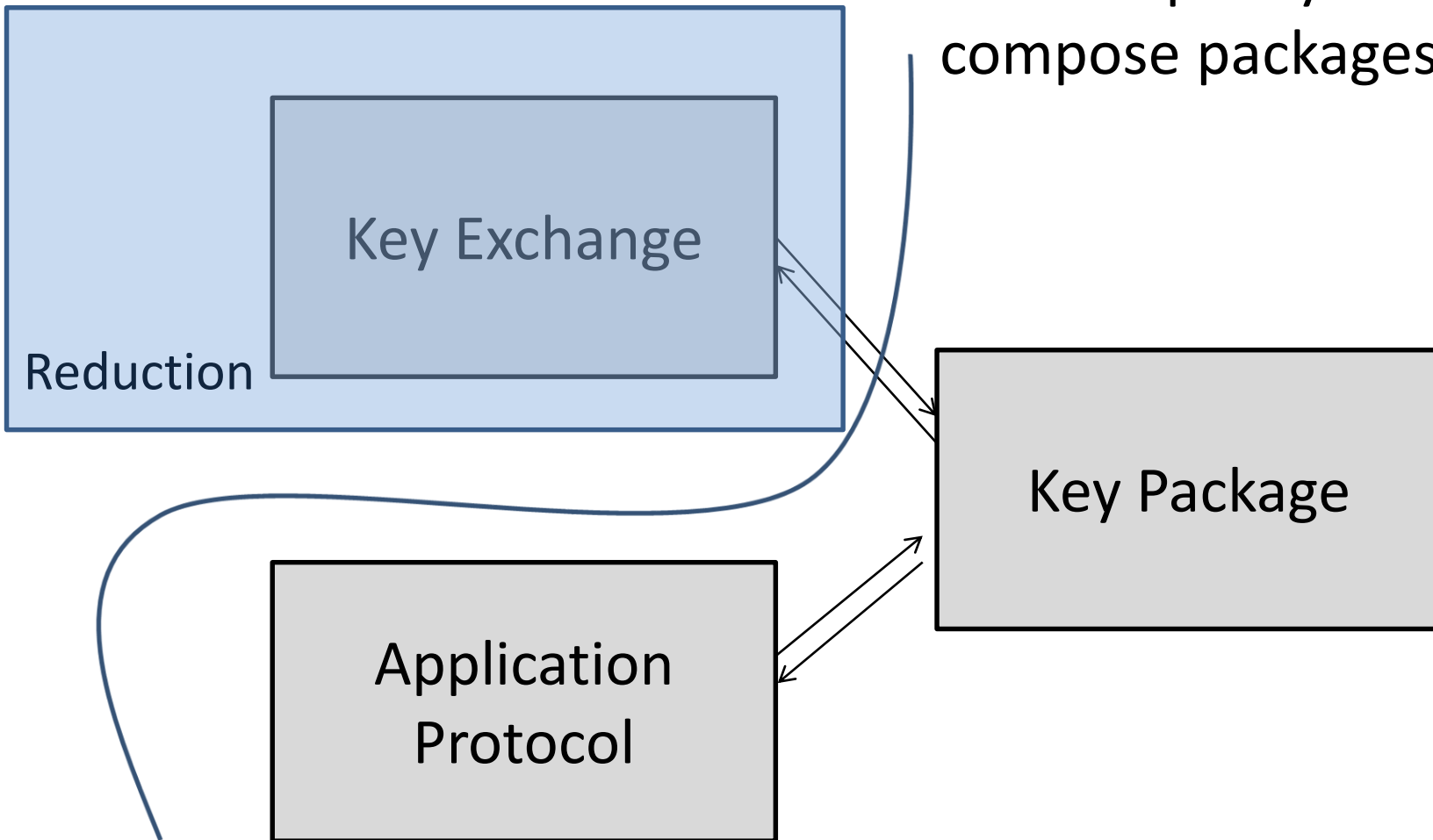
Idea 2: Specify rules to  
compose packages



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Idea 2: Specify rules to compose packages

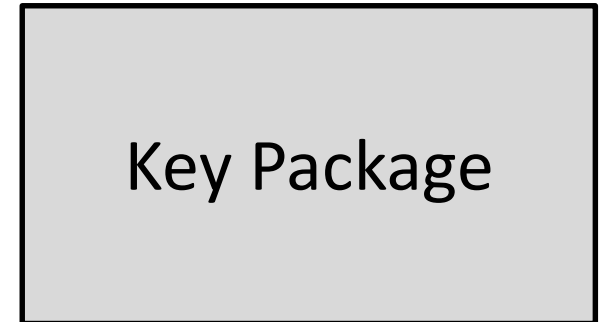


The reduction is defined *automatically* and *precisely*.  
How? The main focus of the paper is package composition.

Bracket operator for  
parallel composition

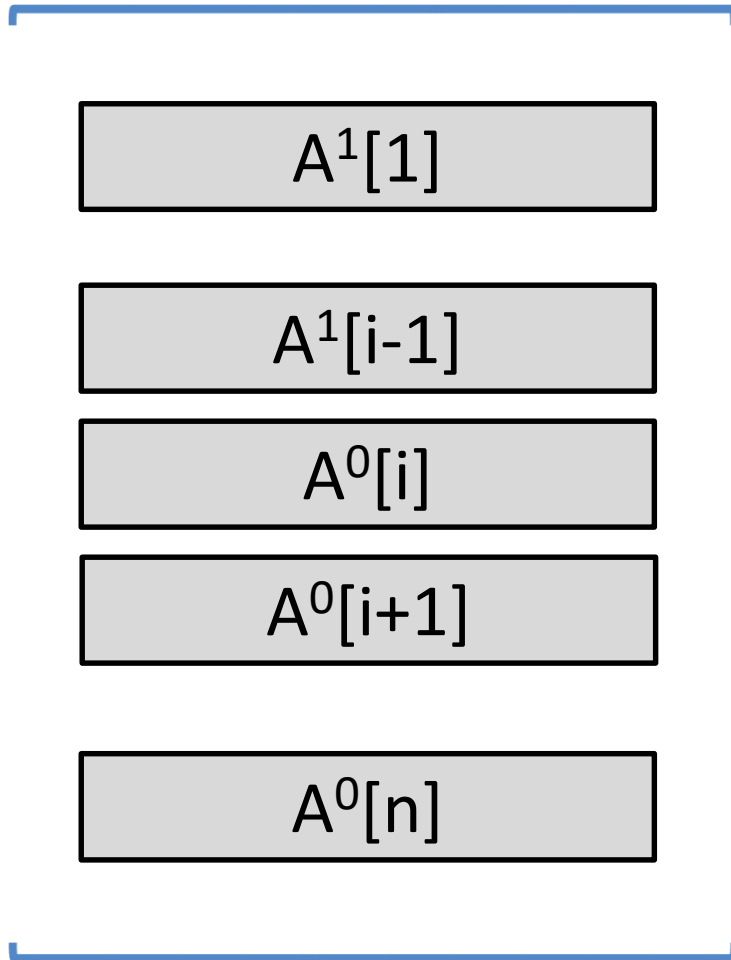


Circle operator for  
packages that interact



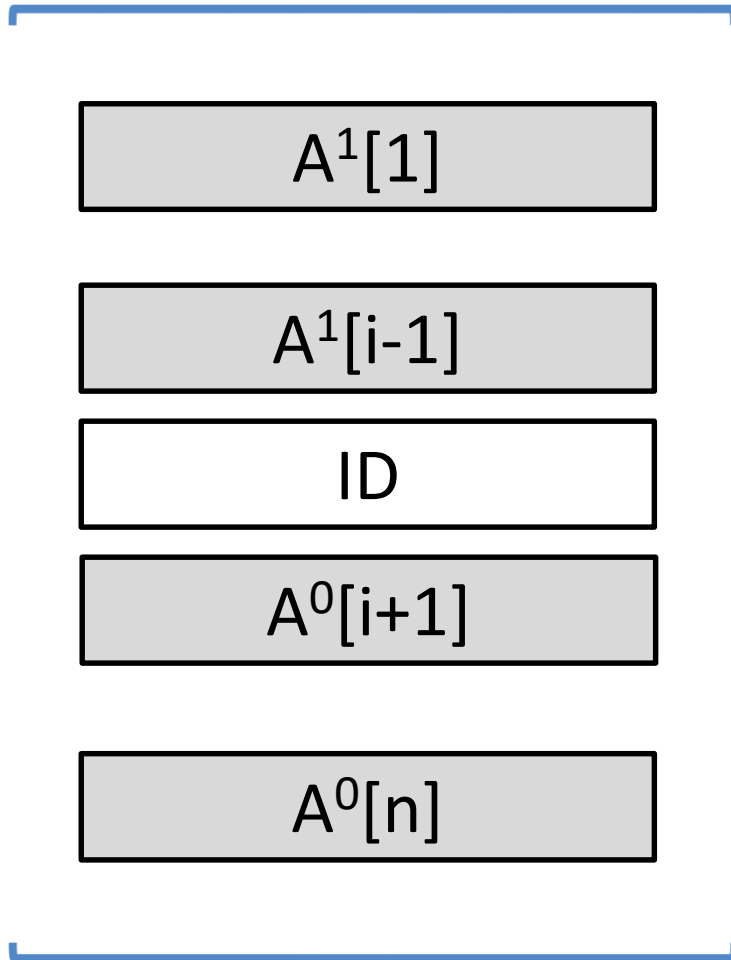
# Hybrid

Idea 3: Specify algebraic rules



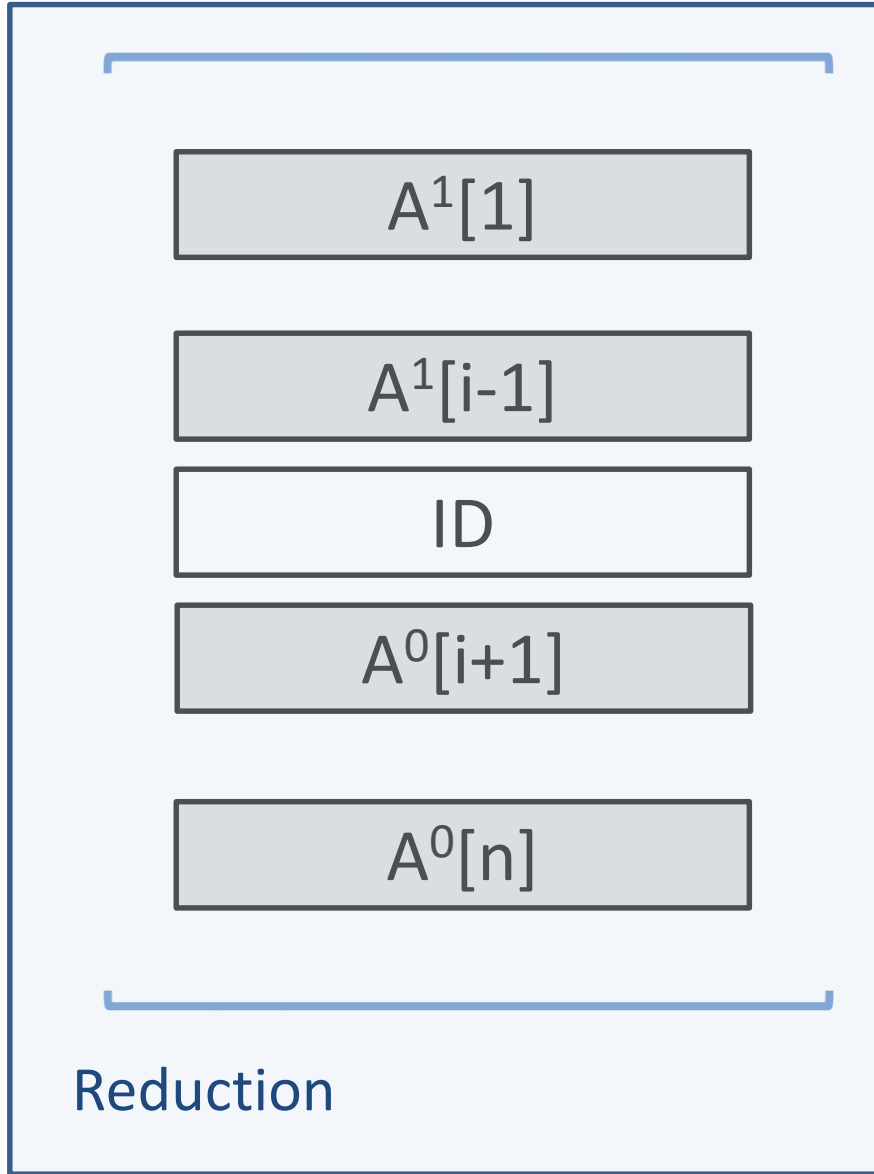
# Hybrid

Idea 3: Specify algebraic rules





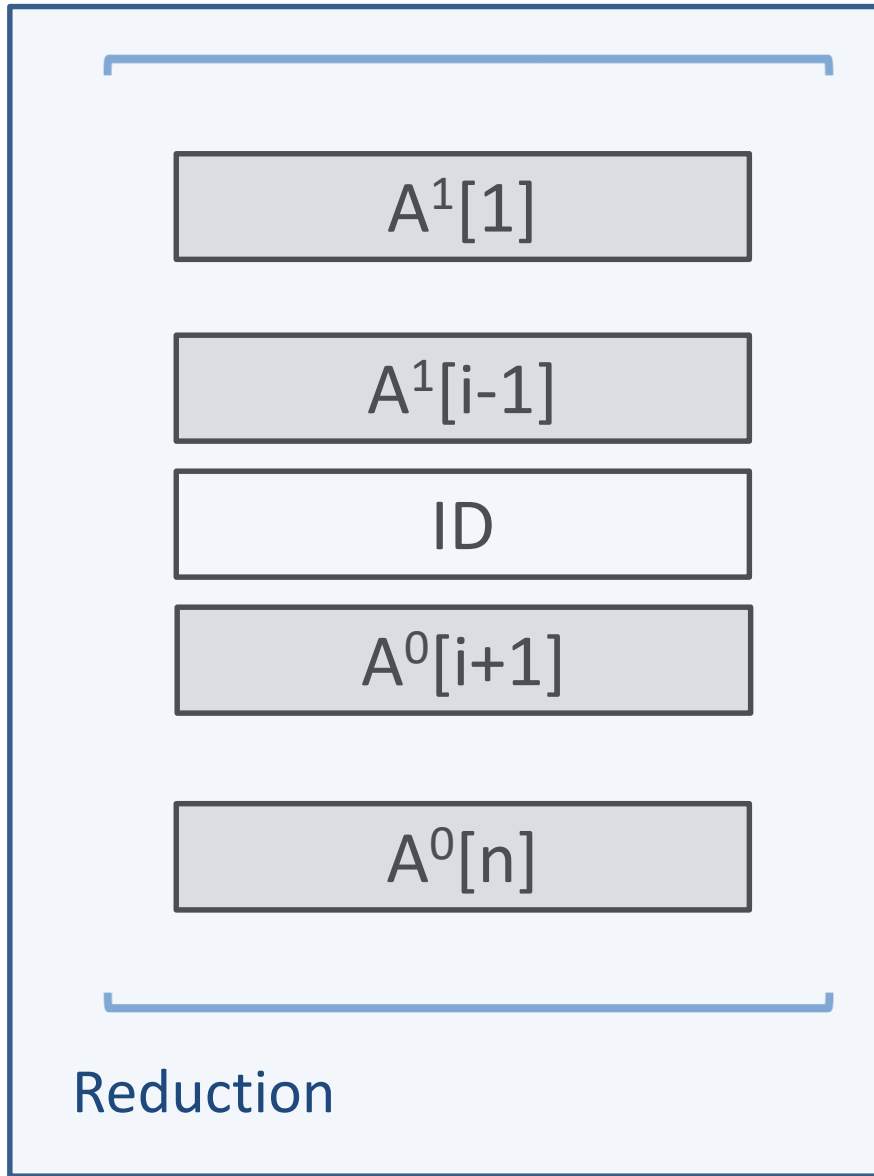
# Hybrid



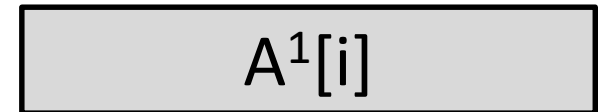
Idea 4: Automatic precise description of reductions



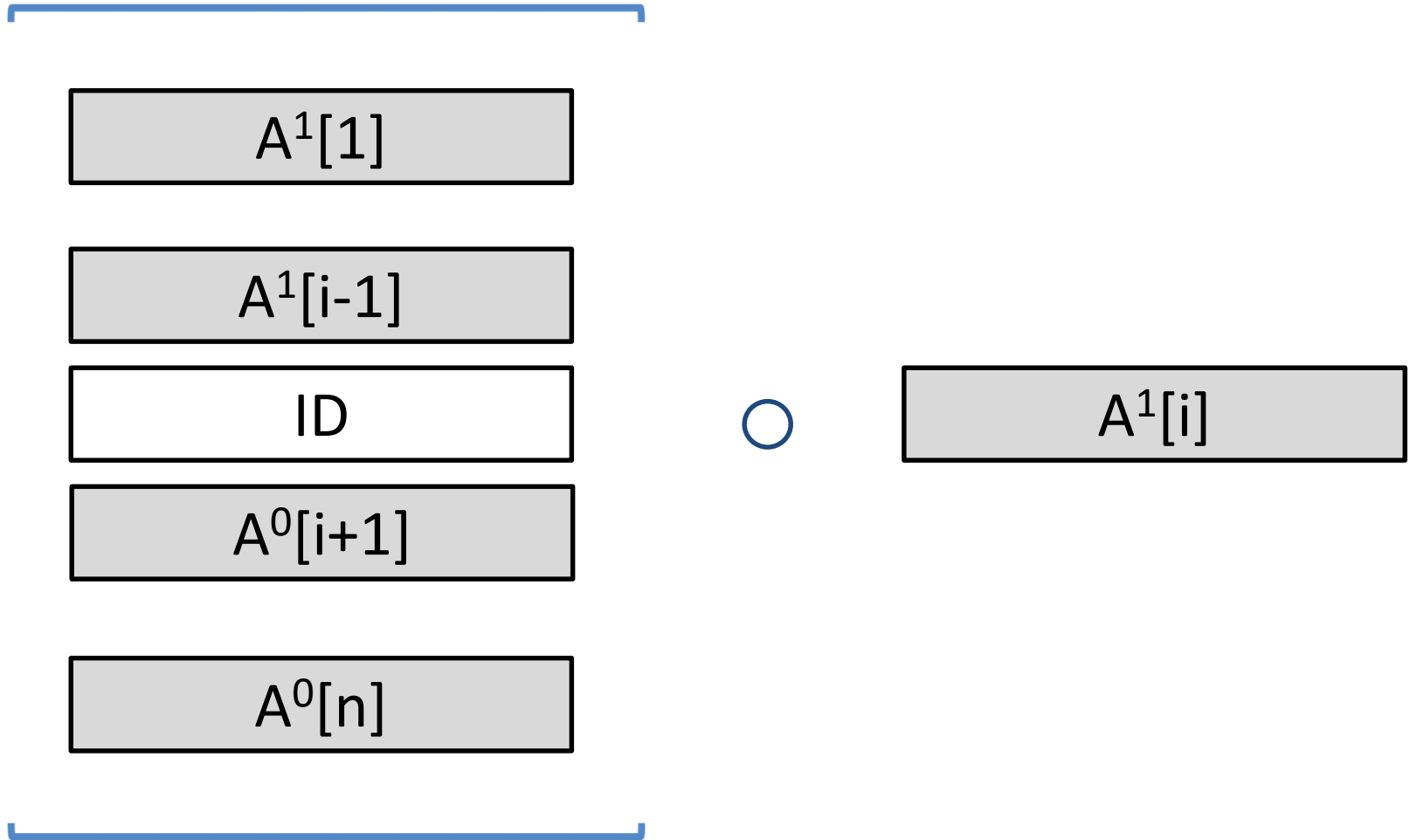
# Hybrid



Idea 4: Automatic precise description of reductions



# Hybrid



# Hybrid

$A^1[1]$

$A^1[i-1]$

$A^1[i]$

$A^0[i+1]$

$A^0[n]$

# Motivation: Simple steps are

- a) little work
- b) precise
- c) human-verifiable

# Usability

Mike Rosulek uses some ideas and especially *similar notation* in the draft of his book  
“The Joy of Cryptography”  
which he has used in his *undergraduate*  
classes for years.

# Our Hope:

- a) Use method to prove TLS 1.3
- b) Use method for meta-reductions
- c) Make key exchange papers readable again
- d) Suffer less, understand more 😊

# Request/Suggestion

If you suffer from writing seemingly simple proof steps or from making them accessible to readers, check whether our notation can help.

If you have the same struggle in teaching, check whether Mike's book can help you.



# Selection of Acknowledgements & Inspirations

- Universal composability, Ran Canetti
- Random systems, abstract crypto, constructive crypto, Ueli Maurer & Renato Renner
- miTLS, Microsoft Research & Inria Paris
- Pi-Calculus

We put existing ideas together with a focus on *proofs* and real-life protocol proofs in mind.

Now on ePrint:

# State-Separating Proofs A Reduction Methodology for Real-World Protocols

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Maybe, it can help you, too 😊